## **Evaluating Patient Level Costs**

Statistical Considerations in Health Economic Evaluations

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## Outline

- Part 1. Univariate analysis
  - Policy relevant parameter for CEA
  - Cost data 101
  - T-tests
  - Response to the violation of normality
  - Primer on log cost
  - Why do different statistical tests lead to different inferences?
- Part 2. Multivariable analysis



## Policy Relevant Parameter for CEA (I)

- Policy relevant parameter: differences in the arithmetic, or sample, mean
  - In welfare economics, a project is cost-beneficial if the winners from any policy gain enough to be able to compensate the losers and still be better off themselves
    - Thus, we need a parameter that allows us to determine how much the losers lose, or cost, and how much the winners win, or benefit
  - From a budgetary perspective, decision makers can use the arithmetic mean to determine how much they will spend on a program



## Policy Relevant Parameter for CEA (II)

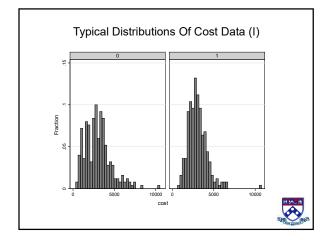
- Other summary statistics such as median cost may be useful in describing the data, but do not provide information about the difference in cost that will be incurred or the cost saved by treating patients with one therapy versus another
  - They thus are not associated with social efficiency
- Lack of symmetry of cost distribution does not change fact that we are interested in the arithmetic mean
- Evaluating some other difference, be it in medians or geometric means, simply because the cost distribution satisfies the assumptions of the tests for these statistics, may be tempting, but does not answer the question we are asking



## Cost Data 101

- Common feature of cost data is right-skewness (i.e., long, heavy, right tails)
- · Data tend to be skewed because:
  - Can not have negative costs
  - Most severe cases may require substantially more services than less severe cases
  - Certain events, which can be very expensive, occur in a relatively small number of patients
    - A minority of patients are responsible for a high proportion of health care costs

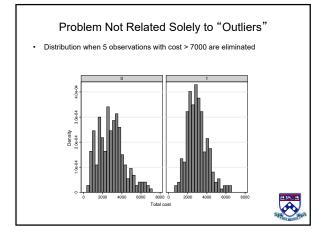




## Typical Distribution Of Cost Data (II)

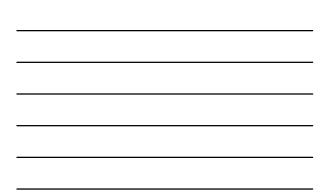
- · Heavy tails vs. "outliers"
  - Distributions with long, heavy, right tails will have means that differ from the median
    - Median is not a better measure of the costs on average than is the mean







	Full S	ample	Trimmed	(3*SD) *
	Group 0	Group 1	Group 0	Group 1
Mean	3015	3040	2927	3010
Median	2826	2901	2816	2885



#### Univariate And Multivariable Analyses Of Economic Outcomes

- Analysis plans for economic assessments should routinely include univariate and multivariable methods for analyzing the trial data
- Univariate analyses are used for the predictors of economic outcomes
  - Demographic characteristics, clinical history, length of stay, and other resource use before entry of study participants into the trial
- Univariate and multivariable analyses should be used for the economic outcome data
  - Total costs, hospital days, quality-adjusted life years



## Univariate Analysis Of Costs

- Report:
  - Arithmetic means and their difference
    - Economic analysis is based on differences in arithmetic mean costs (because n x mean = total), not median costs; thus means are the statistic of interest
  - Measures of variability and precision, such as:Standard deviation
    - Quantiles such as 5%, 10%, 50%,...
  - An indication of whether or not the difference in arithmetic means
    - Occurred by chance and is economically meaningful



# Univariate Analysis: Parametric Tests Of Raw Means

- Usual starting point: T-tests and one way ANOVA
   Used to test for differences in arithmetic means in
  - total costs, QALYS, etc.
  - Makes assumption that the costs are normally distributed
  - Normality assumption is routinely violated for cost data, but in large samples t-tests have been shown to be robust to violations of this assumption when:
    - Samples moderately large
    - Samples are of similar size and skewness
    - Skewness is not too extreme



## Responses To Violation Of Normality Assumption

- Adopt nonparametric tests of other characteristics of the distribution that are not as affected by the nonnormality of the distribution ("biostatistical" approach)
- Transform the data so they approximate a normal distribution ("classic econometric" approach)
- Adopt tests of arithmetic means that avoid parametric assumptions (most recent development)
- OBSERVATION: If we abandon statistical testing of the arithmetic mean because distributional assumptions of the t-test are violated, does not imply that we are not interested in differences in the arithmetic mean



#### Response 1: Non-parametric Tests of Other Characteristics of the Distribution

- Rationale: Can analyze the characteristics that are not as affected by the nonnormality of the distribution
  - Wilcoxon rank-sum test
  - Kolmogorov-Smirnov test



#### Potential Problem with Testing Other Characteristics of the Distribution

- Tests indicate that some measure of the cost distribution differs between the treatment groups, such as its shape or location, but not necessarily that the arithmetic means differ
- The resulting p-values need not be applicable to the arithmetic mean
- While we might decide to compare cost by use of tests like the Mann-Whitney U test, the numerator and denominator of the cost-effectiveness ratio should never be represented as a difference in median cost or effect



#### Response 2: Transform the Data

- Transform costs so they approximate a normal distribution
  - Common transformations
    - Log (arbitrary additional transformations required if any observation equals 0)
    - Square root
  - Estimate and draw inferences about differences in transformed costs



#### Estimates and Inferences Not Necessarily Applicable to Arithmetic Mean

- Goal is to use these estimates and inferences to estimate and draw inferences about differences in untransformed costs
  - Estimation: Simple exponentiation of mean of log costs results in geometric mean, which is a biased estimate of the arithmetic mean
    - Need to apply smearing factor
  - Inference: On the retransformed scale, inferences about the log of costs translate into inferences about differences in the geometric mean rather than the arithmetic mean



Primer On The Log Transformation Of Costs



Raw Cost	Group 2	Group 3
Obs: 1	15	35
2	45	45
3	75	55
Arith mean	45	45
Geom mean	36.933	44.247
Log of arith mean	3.806662	3.806662
Log Cost		
Obs: 1	2.70805	3.555348
2	3.806662	3.806662
3	4.317488	4.007333
Arith mean of logs	3.610734	3.789781
Exp(mean In)	36.993	44.247



## Primer On The Log Transformation Of Costs

- Observation: Simple exponentiation of the mean of the logs yields the geometric mean of costs, which in the presence of variability in costs (variance, skewness, kurtosis) is a biased estimate of the arithmetic mean
  - All else equal, the greater the variance, the skewness, or kurtosis, the greater the downward bias of the exponentiated mean of the logs
  - e.g.,  $(25 * 30 * 35)^{0.333} = 29.7196$  $(10 * 30 * 50)^{0.333} = 24.6621$  $(5 * 30 * 55)^{0.333} = 20.2062$ 
    - $(1 * 30 * 59)^{0.333} = 12.0664$
- "Smearing" factor attempts to eliminate bias from simple exponentiation of the mean of the logs



## Retransformation Of The Log Of Cost (I)

• Duan's common smearing factor:

$$\Phi = \frac{1}{N} \sum_{i=1}^{N} e^{(Z_i - \hat{Z}_i)}$$

where in univariate analysis, 2 , = the group mean
Most appropriate when treatment group variances are equivalent



Group	Observ	In	<b>z</b> -Ŷ	e <sup>(z, - ź,)</sup>
2	1	2.708050	-0.9026834	0.4054801
2	2	3.806663	0.1959289	1.216440
2	3	4.317488	0.7067545	2.027401
Mean, 2		3.610734		
3	1	3.555348	-0.2344332	0.7910191
3	2	3.806663	0.0168812	1.017025
3	3	4.007333	0.2175519	1.24303
Mean, 3		3.789781		
Smear			c	1.116732



Retransform	nation formula		
	$E(\overline{Y}_2) =$ nation $E(\overline{Y}_3) =$	• Φ e <sup>(Ž<sub>2</sub>)</sup>	
Retransform	nation $E(\overline{Y}_3) =$	$\Phi e^{(Z_3)}$	
Group	Φ	e <sup>(In)</sup>	Predicted cost
2	1.116732	36.993	41.3
3	1.116732	44.247	49.4

## Common Smearing Retransformation (II)

- Why are the retransformed subgroup-specific means --41.3 and 49.4 -- so different from the untransformed subgroup means of 45?
- Because the standard deviations of the subgroups' logs are substantially different

SD<sub>2</sub> = 0.8224; SD<sub>3</sub> = 0.2265

- The larger standard deviation for group 2 implies that compared with the arithmetic mean, its geometric mean has greater downward bias than does the geometric mean for group 3
- Thus, multiplication of the 2 groups' geometric means by a common smearing factor cannot give accurate estimates for both groups' arithmetic means

## Log Transformations and Normal Assumptions

- Log transformations and normal assumptions:
  - If met, t-test of the log may be more efficient than ttest of cost
  - If not met there are no efficiency gains
  - In either case, retransformation translates differences in variance, skewness, and kurtosis into differences in means



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Subgroup-specific Smearing Factors (I)

- Manning has shown that in the face of heteroscedasticity – i.e., differences in variance -- use of a common smearing factor in the retransformation of the predicted log of costs yields biased estimates of predicted costs
- We obtain unbiased estimates by use of subgroupspecific smearing factors
- Manning's subgroup-specific smearing factor:

$$\Phi_j = \frac{1}{N_j} \sum_{i=1}^{N_j} e^{(Z_{ij} - \hat{Z}_j)}$$

)	<b>e</b> <sup>(z<sub>i</sub> - <math>\hat{z}_i</math>)</sup>	z, - 2,	In	Observ	Group
01	0.405480	-0.9026834	2.708050	1	2
40	1.216440	0.1959289	3.806663	2	2
01	2.02740	0.7067545	4.317488	3	2
44	1.21644	(	3.610734		Mean, 2
91	0.791019	-0.2344332	3.555348	1	3
25	1.017025	0.0168812	3.806663	2	3
03	1.24303	0.2175519	4.007333	3	3
45	1.017024	- <	3.789781		Mean, 3



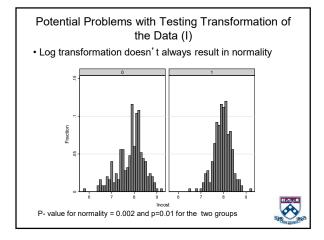
			,
Retrans	formation formu	las	
	$E(\overline{Y}_2) =$	$\Phi_2 \ \mathbf{e}^{(\overline{Z}_2)}$	
	$E(\overline{Y}_3) =$	$\Phi_3 e^{(\overline{Z}_3)}$	
Retrans	formation		
		e <sup>(In)</sup>	Predicted cost
Group	Φ <sub>i</sub>	U	
Group 2	Φ <sub>i</sub> 1.21644	36.993	45.00
•	I		45.0



Subgroup-specific Smearing Retransformation (II)

- All else equal, in the face of differences in variance (or skewness or kurtosis), use of subgroup-specific smearing factors yield unbiased estimates of subgroup means
- Use of separate smearing factors eliminates efficiency gains from log transformation, because we cannot assume that p-value derived for the log of cost applies to the arithmetic mean of cost







# Potential Problems with Testing Transformation of the Data (II)

- When we use a t-test to evaluate log cost, the resulting p-value has direct applicability to the difference in the log of cost
- It generally also applies to the difference in the geometric mean of cost (i.e., we see similar p-values for the difference in the log and the difference in the geometric mean)
- The p-value for the log may or may not be directly applicable to the difference in arithmetic mean of untransformed cost



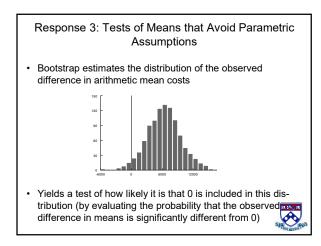
# Potential Problems with Testing Transformation of the Data (III)

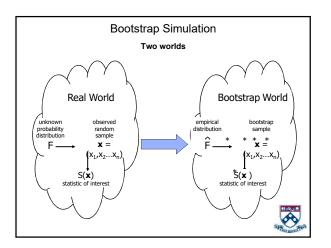
- Whether the p-value for the log is applicable to the difference in the arithmetic mean of untransformed cost depends on whether the two distributions of the log are normal and whether they have equal variance and thus standard deviation
  - If log cost is normally distributed and if the variances are equal, inferences about the difference in log cost are generally applicable to the difference in arithmetic mean cost
  - If log cost is normally distributed and if the variances are unequal, inferences about the difference in log cost generally will not be applicable to the difference in arithmetic mean cost

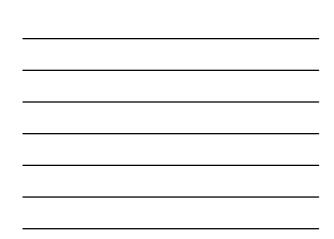
## Potential Problems with Testing Transformation of the Data (IV)

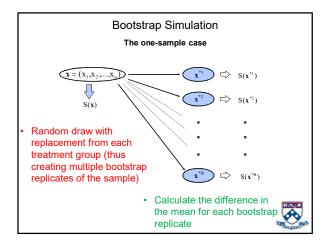
- For economic analysis, the outcome of interest is the difference in untransformed costs (e.g., "Congress does not appropriate log dollars. First Bank will not cash a check for log dollars")
- Thus, the results on the transformed scale must be retransformed to the original scale
- "There is a very real danger that the log scale results may provide a very misleading, incomplete, and biased estimate...on the untransformed scale, which is usually the scale of ultimate interest" (Manning, 1998)
- "This issue of retransformation...is not unique to the case of a logged dependent variable. Any power transformation of y will raise this issue"









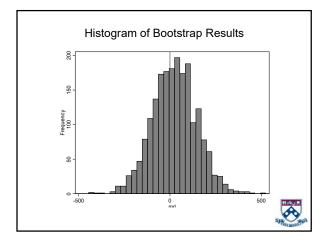




## Bootstrap: Non-parametric and Parametric Tests

- Nonparametric tests
  - P-value: count the number of replicates for which the difference is above and below 0 (yielding a 1-tailed test of the hypothesis of a cost difference)
  - CI: Order the differences from highest to lowest; identify the difference for the replicates that represent the  $2.5^{th}$  and  $97.5^{th}$  percentiles
- Parametric tests:
  - Because each bootstrap replicate represents a mean difference, when we sum the replicates, the reported "standard deviation" is the standard error
    - Difference in means / SE = t statistic
    - Difference in means <u>+</u> 1.96 SE = 95% CI







	Group 0	Group
Arith Mean	3015	304
Std. Dev.	1582.802	1168.73
Quantiles		
5%	899	142
25%	1819	2226
50%	2825.5	2900.
75%	3752	360-
95%	6103	508
Skewness	1.03501	1.525386
Kurtosis	4.910192	9.234913
Geom Mean	2600.571	2835.971
Mean In	7.8634864	7.9501397
SD In	.57602998	.37871479
Obs	250	250



ivariate Tests of t Cost
P-value 95% CI
25.00 SE: 124.44
0.8409 -220 to 270
0.8600 -218 to 275
0.3722
0.0017
0.05
Sqrt
0.2907
0.0000



# Why Do Different Statistical Tests Lead To Different Inferences?

- The tests are evaluating differences in different statistics
  - T-test of untransformed costs indicates we cannot infer that the arithmetic means are different
  - Bootstrap leads to same (lack of) inference and does not make the normality assumption
  - Wilcoxon rank-sum test also leads to the same inference, but its p-value relates more to the probability that the medians differ
  - T-test of log costs indicates we can infer that the mean of the logs are different, and thus the geometric means of cost are different
  - Kolmogorov-Smirnov test indicates we can infer the distributions are different



#### Univariate Analysis: Summary/Conclusion (I)

- Cost-effectiveness ratios ( $\Delta C / \Delta E$ ) and NMB ([WTP  $\Delta E$ ]  $\Delta C$ ) require an estimate of  $\Delta C$  and  $\Delta E$ , the differences in arithmetic means
- If arithmetic means are the most meaningful summary statistic of costs, we should test for significant differences in arithmetic mean costs
  - Parametric test of means
  - Non-parametric test of means (e.g., bootstrap methods)



#### Univariate Analysis: Summary/Conclusion (II)

- Because of distributional problems related to evaluating the arithmetic mean, there has been a growing use of nonparametric tests such as Wilcoxon and KS tests
  - Problem: Their use divorces hypothesis testing from estimation
    - i.e., we want to 1) estimate the magnitude of the difference in arithmetic means and 2) test whether that difference was observed by chance
    - Use of tests of medians or distributions to address the second task does not help with the first task
- Tests of transformed variables such as the log or square root pose similar problems



## Outline (2)

- Part 1. Univariate analysis
- Part 2. Multivariable analysis
  - Ordinary least squares
  - Untransformed cost
  - Log of cost
  - General linear models (GLM)
  - Diagnostic tests
- · Summary



#### Multivariable Analysis Of Economic Outcomes (I)

- Even if treatment is assigned in a randomized setting use of multivariable analysis may have added benefits:
  - Improves the power for tests of differences between groups (by explaining variation due to other causes)
  - Facilitates subgroup analyses for cost-effectiveness (e.g., more/less severe; different countries/centers)
  - Variations in economic conditions and practice pattern differences by provider, center, or country may have a large influence on costs and the randomization may not account for all differences
  - Added advantage: Helps explain what is observed (e.g., coefficients for other variables should make sense economically)



## Multivariable Analysis Of Economic Outcomes (II)

 If treatment is not randomly assigned, multivariable analysis is necessary to adjust for observable imbalances between treatment groups, but it may NOT be sufficient



#### Multivariable Techniques Used for the Analysis of Cost

- Common Techniques
  - Ordinary least squares regression predicting costs after randomization (OLS)
  - Ordinary least squares regression predicting the log transformation of costs after randomization (log OLS)
     Generalized Linear Models (GLM)

#### · Other Techniques:

- Generalized Gamma regression (Manning et al.
- Journal of Health Economics 2005)
- Extended estimating equations (Basu and Rathouz Biostatistics 2005)

## Multivariable Analysis

- Different multivariable models make different assumptions
  - When assumptions are met, coefficient estimates will have many desirable properties
  - With cost analysis, assumptions are often violated, which may produce misleading or problematic coefficient estimates
    - · Bias (consistency)
    - Efficiency (precision)



## Ordinary Least Squares (OLS)

 $Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k + \varepsilon$ 

- Advantages
  - Easy
  - No retransformation problem (faced with log OLS)
  - Marginal/Incremental effects easy to calculate
- Disadvantages
  - Not robust:
    - In small to medium sized data set
    - In large datasets with extreme observations
  - Can produce predictions with negative costs



## Log Of Costs Ordinary Least Squares (log OLS)

$$InY = \alpha + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k + \varepsilon$$

- · Advantages
  - Widely known transformation for costs
  - Common in the literature
  - Reduces robustness problem
  - Improves efficiency
- Disadvantages
  - Retransformation problem can lead to bias
  - Coefficients not directly interpretable
  - Not easy to implement
  - Residual may not be normally distributed even after log transformation



## Problems with 'Typical" Methods

- · Problems with OLS
  - Not robust
  - Can produce predictions with negative cost
- · Problems with log OLS
  - Retransformation problem can lead to bias
  - Coefficients not directly interpretable
  - Residual may not be normally distributed even after log transformation
- · More generally:
  - Assume constant variance
  - Assume E(In(y)/x)= $\Sigma\beta_iX_i$



## Generalized Linear Models (GLM)

- GLM models have the advantages of the log models, but
  - Don't require normality or homoscedasticity,
  - Evaluate the log of the mean, not the mean of the logs, and thus
  - Don't raise problems related to retransformation from the scale of estimation to the raw scale
- To build them, we must identify a "link function" and a "family" (based on the data)



## GLM Relaxes OLS Assumptions

- Ability to choose among different families relaxes
   assumption of constant variance
  - Gauss: constant variance
  - Poisson: variance proportional to mean
  - Gamma: variance proportional to square of mean
  - Inverse gauss: variance proportional to cube of mean
- Ability to choose among different links relaxes assumption that y/x= Σβ<sub>i</sub>X<sub>i</sub> (OLS) or E(ln(y)/x)=Σβ<sub>i</sub>X<sub>i</sub> (Log OLS)

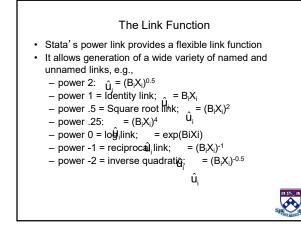


#### The Link Function

• Link function directly characterizes how the linear combination of the predictors is related to the prediction on the original scale

– e.g., predictions from the identity link -- which is used in OLS -- equal:  $\hat{Y}_i = \beta_i X_i$ 





## The Log Link

- Log link is most commonly used in literature
- When we adopt the log link, we are assuming:  $ln(E(y/x))=X\beta$
- GLM with a log link differs from log OLS in part because in log OLS, we are assuming:  $E(ln(y)/x)=X\beta$
- $ln(E(y/x) \neq E(ln(y)/x)$ i.e. log of the mean  $\neq$  mean of the log costs



Variable	Group 1	Group 2
Observations		
1	15	35
2	45	45
3	75	55
Arithmetic mean	45	45
Log, arith mean cost	3.806662	3.806662 *
Natural log		
1	2.70805	3.555348
2	3.806662	3.806662
3	4.317488	4.007333
Arith mean, log cost	3.610734	3.789781 †



Variable	Coefficient	SE	z/T	<i>p</i> value
GLM, gam	ma family, log lir	nk		
Group 2 🕻	0.000000	0.405730	0.00	1.000
Constant	3.806662	0.286894	13.27	0.000
Log OLS				
Group 2 🕻	0.179048	0.492494	0.36	0.74
Constant	3.610734	0.348246	10.32	0.000



## Selecting a Link Function

- While log link is most commonly used in literature, need not be the best fitting link
- There is no single test that identifies the appropriate link
- · Instead can employ multiple tests of fit
  - Pregibon link test checks linearity of response on scale of estimation
  - Modified Hosmer and Lemeshow test checks for systematic bias in fit on raw scale
  - Pearson's correlation test checks for systematic bias in fit on raw scale
  - Ideally, all 3 tests will yield nonsignificant p-values



#### The Family

- Specifies the distribution that reflects the mean-variance relationship
- Currently, families for continuous data available in Stata include:
  - Gaussian (constant variance)
  - Poisson (variance is proportional to mean)
  - Gamma (variance is proportional to square of mean)
  - Inverse gaussian (variance is proportional to cube of mean)
- Use of the poisson, gamma, and inverse Gausian families relaxes the assumption of homoscedasticity

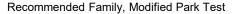


#### Selecting a Family

- Modified Parks test is a "constructive" test that recommends a family given a particular link function
- Implemented after GLM regression that uses the particular link
- The test predicts the square of the residuals (res<sup>2</sup>) as a function of the log of the predictions (Inyhat) by use of a GLM with a log link and gamma family to

## Stata code

- glm res<sup>2</sup> lnyhat,link(log) family(gamma), robust
- If weights or clustering are used in the original GLM, same weights and clustering should be used for modified Park test



- Recommended family derived from the coefficient for Inyhat:
  - If coefficient ~=0, Gaussian
  - If coefficient ~=1, Poisson
  - If coefficient ~=2, Gamma

rerunning analysis

- If coefficient ~=3, Inverse Gaussian or Wald
- Given the absence of families for negative coefficients:

   If coefficient ≤ -0.5, consider subtracting all observations from maximum-valued observation and



## Stata and SAS Code

STATA code:

glm y x, link(linkname) family (familyname)

General SAS code (not appropriate for gamma family / log link):

proc genmod;

model y=x/ link=linkname dist=familyname; run;



## SAS Code for a Gamma Family / Log Link

- When running gamma/log models, the general SAS code drops observations with an outcome of 0
- If you want to maintain these observations and are predicting y as a function of x (M Buntin): proc genmod;

a = \_mean\_;

b = \_resp\_;

d = b/a + log(a)

variance var = a<sup>2</sup>

deviance dev =d;

model y = x / link = log; run;



Stata Commands: Mod	ified Park Test
. gen res2 = ((cost-yhat)^2) . gen lnyhat = ln(yhat)	
. glm res2 lnyhat , link(log) family(gam	ma) robust nolog
Generalized linear models Optimization : ML: Newton-Raphson	No. of obs = 200 Residual df = 198 Scale parameter = 5.37055
Deviance = 556.0966603 Pearson = 1063.368955	*
Variance function: $V(u) = u^2$ Link function : $g(u) = ln(u)$ Standard errors : Sandwich	[Gamma] [Log]
Log pseudo-likelihood = -3667.729811 BIC =-492.9701783	AIC = 36.6973
Robust res2   Coef. Std.Err. z P>	z  [95% Conf. Intervenue

Stata Output, Modified Park Test			
. test lnyhat==1			
( 1) [res2]lnyhat	= 1		
chi2( 1) Prob > chi2 . test lnyhat==2	= 0.10 = 0.7488 → Implies poisson		
( 1) [res2]lnyhat	= 2		
chi2( 1) Prob > chi2 . test lnyhat==3	= 3.88 = 0.0487 → Not gamma		
( 1) [res2]lnyhat	= 3		
chi2( 1) Prob > chi2	= 13.11 = 0.0003 → Not inverse gaussian		

## GLM Comments (I)

- Advantages
  - Relaxes normality and homoscedasticity assumptions
  - Consistent even with mis-specification of family so long as link function and covariates are specified correctly
  - Gains in precision from estimator that matches data generating mechanism
  - Avoids retransformation problems of log OLS models



### GLM Comments (II)

## Disadvantages

- Can suffer substantial precision losses
  - If heavy-tailed (log) error term, i.e., log-scale residuals have high kurtosis (>3)
  - If family is misspecified



## Retransformation (I)

- GLM avoids the problem that simple exponentiation of the results of log OLS yields biased estimates of predicted costs
- It does not avoid the other complexity of nonlinear retransformations (also seen in log OLS models):
  - On the transformed scale, the effect of the treatment group is estimated holding all else equal; however, retransformation (to estimate costs) reintroduces the covariate imbalances



## Recycled Predictions (I)

- Do not use the means of the covariates to avoid the reintroduction of covariate imbalance, because the mean of nonlinear retransformations does not equal the linear retransformation of the mean
- Rather, use the method of recycled predictions to create an identical covariate structure for the two groups by:
  - Coding everyone as if they were in treatment group 0 and predicting  $\hat{Z}_{_0}$
  - Coding everyone as if they were in treatment group 1 and predicting  $\hat{Z}_{\!_1}$



GLM Model Output			
*****glm model (poisson/log) . glm cost treat \$ivar, family(poisson) link(log)			
Generalized linear models Optimization: ML: Newton-Raphson Deviance = 700567.946	No. of obs = 200 Residual df = 193 Scale parameter = 1 (1/df) Deviance = 3629.886		
	(1/df) Pearson = 4101.325 [Poisson] [Log]		
Log likelihood = -351346.9719 BIC = 699545.3708	AIC = 3513.54		
cost   Coef. Std. Err. z	<pre>P&gt; z  [95% Conf. Interval]</pre>		
ejfract  0081781 .0001135 -72.07 sex  0721448 .0016935 -42.60 etiology   .2498528 .0015617 159.99	0.000 .0081507 .0084472 0.00000840060079557 0.00007546390688256 0.000 .2467919 .2529137 0.000 .0416499 .0509398		
	South States and States		

## 



#### **Extended Estimating Equations**

- Basu and Rathouz (2005) have proposed use of extended estimating equations (EEE) which estimate the link function and family along with the coefficients and standard errors
- Tends to need a large number of observations (thousands not hundreds) to converge
- Currently can't take the results and use them with a simple GLM command (makes bootstrapping resulting models cumbersome)



## Special Cases (I)

- A substantial proportion of observations have 0 costs
   May pose problems to regression models
  - Commonly addressed by developing a "two-part" model in which the first part predicts the probability that the costs are zero or nonzero and the second part predicts the level of costs conditional on there being some costs
    - 1st part : Logit or probit model
    - 2nd part : GLM model



## Special Cases (II)

- · Censored costs
  - Results derived from analyzing only the completed cases or observed costs are often biased
  - Need to evaluate the "mechanism" that led to the missing data and adopt a method that gives unbiased results in the face of missingness

For details see Chapter 6 in Glick HA, Doshi JA, Sonnad SS, Polsky D. Economic Evaluation in Clinical Trials, 2007 (Oxford University Press).



## Multivariate Analysis: Summary/Conclusion

- Use mean difference in costs between treatment groups estimated from a multivariable model as the numerator for a cost-effectiveness ratio
- Establish criteria for adopting a particular multivariable model for analyzing the data prior to unblinding the data (i.e., the fact that one model gives a more favorable result should not be a reason for its adoption)
- Given that no method will be without problems, it may be helpful to report the sensitivity of our results to different specifications of the multivariable model

