Sample Size and Power for Cost-Effectiveness Analysis

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## Outline

- Goals of sample size and power analysis
- Sample size
	- Formula
	- Similarities to and differences from clinical SS&PA
		- Correlation of difference
		- Willingness to pay
		- Standard deviations of cost and effect
- Power
	- Formula
	- Patterns of power
- (Briefly) Where to obtain the data
- (Brierry) Writtle to Jouding the South of Cost-Effectivenes

















#### Goal of Sample Size and Power Calculation

- More generally, sample size and power calculations allow us to conduct experiments with an expected likelihood that at conclusion of experiment we will be able to be confident in resulting comparison of costs and effects
	- e.g., may hypothesize that point estimate for costeffectiveness ratio for therapy A will be 20,000 per **QALY**
	- May want to design an experiment that provides an 80% chance (i.e., power) of concluding with 95% confidence that therapy A is good value when we are willing to pay at most 75,000 per QALY



#### Sample Size / Power

- Sample size calculation
	- Given a desired alpha (α) and power (1-β), proactively manages probability of saying a difference exists when none does
- Type 1 error; False positive; alpha; confidence • Power Analysis
	- - Given a desired alpha and a known sample size, proactively manages probability of saying no difference exists when one does
			- Type 2 error; False negative; (1-Beta); power
- "provides an 80% chance (power) of concluding with 95% confidence (alpha) that therapy is good value"



#### Other Cost-Effectiveness Sample Size Traditions

- Sample size approach described here comes out of frequentist statistical tradition
- Other approaches that have been discussed in costeffectiveness literature include:
	- Bayesian (O'Hagan and Stevens)
	- Value of information (Koerkamp et al.)
	- Opportunity cost (Gafni et al.)
	- Decision model (Willan and O'Brien)





$$
n = \frac{2 (z_{\alpha} + z_{\beta})^2 (sd_c^2 + (W sd_q)^2 - (2 W \rho sd_c sd_q))}{(W\Delta Q - \Delta C)^2}
$$

where n = sample size/group;  $z_\alpha$  and  $z_\beta$  = z-statistics for α (e.g., 1.96) and β (e.g., 0.84) errors; sd = standard deviation for cost (c) and effect (q);  $W =$  maximum willingness to pay we wish to rule out; and  $\rho =$ correlation of difference in cost and effect; and (W∆Q-  $\Delta C$ ) = NMB

www.uphs.upenn.edu/dgimhsr/stat-samps.htm **BASE** 





#### Sample Size Supports Other α / β Pairs

- Yes, 95 participants per group support  $\alpha = 0.05$  and power=0.8
- But what enters formula is sum of  $z_\alpha$  and  $z_\beta$   $(z_\alpha + z_\beta)^2$  $-$  E.g., for α=0.05 and 1-β=0.8, 2.8016 (1.96 + .8416)
- 95 participants per group supports any  $z_\alpha/z_\beta$  pair that has same sum, e.g.,:



#### Null Hypothesis, NMB

- Formula identifies a sample size that provides a 1- β% chance to have 1−α% confidence for rejection of null hypothesis that NMB (NMB =  $WQ - C$ ) calculated by use of W equals 0
	- If assumptions about C, Q, sd<sub>c</sub>, sd<sub>q</sub>, and ρ are correct and if  $\alpha$ =0.05 and 1- $\beta$ =0.8, then with a sample size of 95 per group:
		- In approximately 800 of 1000 repeated experiments, lower limit of 95% confidence interval for difference in NMB will be greater than 0 (therapy represents good value)
		- In approximately 200, 95% confidence intervals will either include 0 or have an upper limit less than 0 (no difference in or bad value)



- Formula also identifies a sample size that provides a 1 β% chance to have 1−α% confidence for rejection of null hypothesis that cost-effectiveness ratio equals W (i.e., that 1−α% confidence interval for cost-effectiveness ratio excludes W)
- Or equivalently, identifies a sample size that provides a 1- β% chance for rejection of null hypothesis that at W, fraction of joint distribution of difference in cost and effect that is acceptable is greater than α/2% and less than 1 − ( α/2)%







# Differences in Formulas

$$
Var_{NMB} = sd_c^2 + (W sd_q)^2 - (2 W \rho sd_c sd_q)
$$

- Variance of NMB more complicated than variance for usual continuous clinical differences
	- Includes ρ, correlation of difference between cost and effect
	- Includes W, decision threshold we are trying to rule out



# $\left(\text{sd}_{c}^{2} + (\text{W sd}_{q})^{2} - (2 \text{W }\rho \text{ sd}_{c} \text{ sd}_{q})\right)$

- Correlation of difference in cost and effect indicates how changes in difference in cost are related to changes in difference in effect
	- Negative (win/win) correlation: larger differences in effects associated with smaller differences in costs
		- e.g., asthma care: reductions in exacerbations leads to lower costs
	- Positive (win/lose) correlation: larger differences in effects are associated with larger differences in costs
		- e.g., life-saving care: increases in stroke survival may lead to higher care costs
- If W is positive, all else equal, FEWER patients are needed when correlation is positive (win/lose) than when correlation is negative (win/win)



#### Effect of Correlation on Sample Size

• If ∆C=200, ∆Q=.01; SDc= 447.845; SDq=.01326715; W=75,000; α=0.05; and 1-β=0.8:





#### Willingness to Pay and Identification of an Appropriate Outcome Measure

- Sample size calculations require stipulation of W for a unit of outcome
- In many medical specialties, researchers use disease specific outcomes
- Can calculate a cost-effectiveness ratio for any outcome (e.g., cost/case detected; cost/abstinence day)
- But to be informative, outcome must be one for which we have recognized benchmarks of cost-effectiveness
	- Argues against use of too disease-specific an outcome for economic assessment



#### W and Point Estimate

- When W is greater than expected point estimate, resulting sample size and power will allow us to be confident about value of MORE EFFECTIVE THERAPY
	- Because confidence statements from these trials will be that point estimate for more effective therapy is less than willingness to pay
- When W is less than expected point estimate, resulting sample size and power are for experiments that allow us to be confident that MORE EFFECTIVE THERAPY is bad value
	- Because confidence statements from these trials will be that point estimate is greater than willingness to pay



## Effect of Willingness to Pay (W)

- As already shown, direction of effect of correlation of difference is known
	- all else equal, more positive correlation, smaller sample size
- For W, no such consistent relationship exists
- Sample size approaches infinity as expected point estimate approaches W
	- $-$  e.g., if W = 75,000, expected ∆C=15,000, and expected ∆Q=0.2, NMB (W ∆Q-C) in denominator of sample size equation approaches 0
- Sample size reaches a minimum at what I refer to as widest definable interval which is uniquely defined for an experiment based on ∆C, SE<sub>c</sub>, ∆Q. Se<sub>q</sub>. and ρ













30,000 50,000 592 567 *151* 75,000 100,000 150,000





# Effect of  $SD_q$  VS  $SD_c$  on Sample Size

- All else equal, increases in  $SD_q$  or  $SD_c$  lead to increases in sample size
- Commonly thought that sample size for costeffectiveness driven more by SD<sub>c</sub> than by SD<sub>q</sub> – If not, why do we commonly need a larger sample for
- cost-effectiveness outcome than for clinical outcome? • However, if willingness to pay is substantially greater
- than SD<sub>c</sub>, percentage changes in SD<sub>q</sub> can have a substantially greater effect on sample size than will equivalent percentage changes in SD $_{\rm c}$



# Sample Size,  $SD_q$ , and  $SD_c$

• Sample size formula is symmetric for SDs of cost and effect except for:

### $sd_c^2 + (W sd_q)^2$

in numerator of equation

- Square of  $SD_q$  is weighted by square of W (e.g.,
	- 75,000<sup>2</sup>); square of  $SD_c$  is unweighted – So long as W SD<sub>q</sub> > SD<sub>c</sub>, SD<sub>q</sub> will have a greater impact on sample size in face of equivalent percentage changes in SD<sub>q</sub> and SD<sub>c</sub>
	- E.g., if W=75,000 and SD<sub>q</sub>=0.2; percentage changes in SD<sub>q</sub> will have larger effect so long as SD<sub>c</sub><15000  $(75,000*0.2)$





• In this case with relatively larger  $SD<sub>c</sub>$ 's, equivalent percentage changes in  $SD_c$  and  $SD_q$  make no difference to required sample size for experiment



 $\Delta$ C=250;  $\Delta$ Q=.0.05; unless otherwise specified, sd<sub>c</sub>= 15,000 and sd<sub>q</sub>=.2; ρ=-.1; W=75,000; α=.05; β=1-.8





## Sample Size Tables, Relatively Small SD<sub>c</sub>

 $\cdot$  In this case with relatively smaller SD $_c$ 's, equivalent percentage changes in  $SD_c$  and  $SD_q$  yield substantially larger shifts in sample size given increases in  $SD<sub>a</sub>$ 



 $\Delta$ C=250;  $\Delta$ Q=0.05; unless otherwise specified, sd<sub>c</sub>= 5000 and  $sd_q = 2$ ; ρ=-.1; w=75,000; α=.05; 1-β=.8

#### Economic Vs Clinical Sample Sizes

- Sample size required to answer economic questions typically considered larger than sample size required to answer clinical questions
	- But not necessarily in all cases
- ∆C and ∆Q are a joint outcome just as differences in nonfatal CVD events and all cause mortality are often combined into a joint outcome
- In same way that we can have more power for joint cardiovascular outcome than either individual outcome alone, we can have more power for cost-effectiveness than we do for costs or effects alone







# Dropout and Sample Size

- Sample size estimates from formula appropriate if we expect no dropout from trial
- If we instead anticipate 10% dropout, divide sample size estimates by 0.9

# Power Formula, Common SDs

• Assuming equal sds and sample sizes, power formula is:

$$
z_{\beta} = \sqrt{\frac{n * (W \Delta Q - \Delta C)^2}{2 \left(s d_c^2 + (W sd_q)^2 - 2 W \rho sd_q sd_c\right)}} - z_{\alpha}
$$

• Result is  $z_{\beta}$ , not power

- To estimate power, use normal distribution table to identify fraction of tail that is to left of  $z_{\beta}$ – Stata (V11+) code: power = normal(zbeta)
	- E.g., -1.96 = 2.5% power; -0.84 = 20% power; 0 =
		- 50% power; .84 = 80% power; 1.28 = 90%

$$
\mathbf{11} \\
$$





























## Dropout and Power

• If we anticipate 10% dropout, we will want to use "effective sample size" (e.g., 0.9 \* 95) when we make our power calculations

#### Where to Obtain Necessary Data?

- When therapies are already in use: Expected differences in outcomes and standard deviations can be derived from feasibility studies or from records of patients
	- Potential sources
		- Medical charts of administrative data sets
		- Patient logs of their health care resource use
		- Asking patients and experts about kinds of care received by those with condition under study
	- Simple correlation between observed costs and effects may be an adequate proxy for measure of correlation used for estimating sample size



## Obtaining Data for Novel Therapies

- For novel therapies, information about magnitude of incremental costs and outcomes may not be available
	- May need to be generated by assumption – Data on standard deviations for those who receive
	- usual care/placebo may be obtained from feasibility studies or patient records
		- May want to assume sd from usual care (or a multiplier) will apply to new therapy, etc.



#### Summary

- Goal of sample size and power calculation for costeffectiveness analysis is to identify likelihood that an experiment will allow us to be confident that a therapy is good or bad value when we adopt a particular willingness to pay
- Sample size and power depend on difference in cost and effect, SD of cost and effect, correlation of difference, our willingness to pay, and our target confidence level



#### Summary (2)

- When we estimate sample size or power, we often do so for varying levels of W
	- Sample size is undefined / power reaches a minimum when W equals point estimate for cost-effectiveness ratio (NMB=0)
- When W is substantially greater than SD for cost, changes in SD for effect generally have greater impact on sample size than do changes in SD for cost
- So long as W>0, positive correlations decrease sample size / increase power



Glick HA. Sample size and power for costeffectiveness analysis (part 1). Pharmacoeconomics. 2011;29;189-98.

Glick HA. Sample size and power for costeffectiveness analysis (part 2). The effect of maximum willingness to pay. Pharmacoeconomics. 2011;29:287- 96.



# Sample Size Formula, SDs Differ

• When SDs differ, formula becomes:

 $(z_\alpha + z_\beta)^2 \left( (\text{sd}_\text{eq}^2 + \text{sd}_\text{ct}^2) + (\text{W}^2 \left( \text{sd}_\text{qq}^2 + \text{sd}_\text{qq}^2) \right) - (2 \text{ W p } (\text{sd}_\text{eq}^2 + \text{sd}_\text{ct}^2)^{0.5} \left( \text{sd}_\text{qq}^2 + \text{sd}_\text{qq}^2 \right)^{0.5} \right)$  $n = \frac{1}{(W \Delta Q - \Delta C)^2}$ 

where n = n/group;  $\text{ta/2}$  and  $\text{tβ}$  = t-statistics for  $\alpha$  and  $\beta$ errors; sd = standard deviation for cost (c) and effect (q); W = maximum willingness to pay one wishes to rule out; and ρ = correlation of difference in cost and effect





#### Unidimensionality vs 2 Dimensionality

- Clinical outcomes typically are unidimentional and sampling uncertainty around these outcomes make sense on real number line
- Cost-effectiveness ratios are 2 dimensional and sampling uncertainty around these ratios can have unexpected properties on real number line
	- E.g., CI for ICER can include -∞ but -∞ needn't represent lower bound of interval; it can include ∞ but ∞ needn't represent upper bound of interval
- Best to view results on 2D cost-effectiveness plane





























Red: confident of bad value All points above W line

Black, not confident of value Too many point on both sides of W line

Blue, confident of good value All points below W line and above X axis

Cyan, confident of dominance All points in lower right quadrant







## 95% CI

Upper left: CI for ∆C

Upper right: CI for NMB

Lower right: 95% confidence ellipse around point on C/E plane defined by ∆C and ∆q (CE for point, not CI for ICER)

Lower left: 95% CI for ICER



#### Confidence Interval for ICER

- Because denominator of ratio can equal 0, there is no SE for ICER
- Thus CAN'T calculate ICER +/- 1.96  $*$  SE<sub>ICER</sub>
- CI for ICER defined as 0, 1, or 2 lines through origin of CE plane that exclude 2.5% of joint distribution of difference in cost and effect
- Fieller's theorem provides parametric equation for calculating these CI:

 $(\Delta$ CΔE-t<sub>α/2</sub><sup>2</sup>ρs<sub>ΔC</sub>s<sub>ΔE</sub>)±([ΔCΔE-t<sub>α/2</sub><sup>2</sup>ρs<sub>ΔC</sub>s<sub>ΔE</sub>]<sup>2</sup>-[ΔE<sup>2</sup>-t<sub>α/2</sub><sup>2</sup>s<sub>ΔE</sub><sup>2</sup>][ΔC<sup>2</sup>-t<sub>α/2</sub><sup>2</sup>s<sub>ΔC</sub><sup>2</sup>])<sup>0.5</sup>  $\Delta E^2$  -t<sub>a/2</sub><sup>2</sup> s<sub> $\Delta E$ </sub><sup>2</sup>



## Net Monetary Benefit (NMB)

- NMB represents a transformation of ICER decision criterion (W > ∆C/∆Q becomes W∆Q - ∆C > 0) which is linear and has a defined SE
	- $SE<sub>NMB</sub> = (SEC<sup>2</sup> + (W SEq<sup>2</sup>) 2 W p SE<sub>c</sub> SE<sub>q</sub>)<sup>0.5</sup>$
- As with other differences, NMB is significant if it's CI excludes 0
- 95%  $Cl_{NMB}$  = NMB +/- 1.96  $*$  SE<sub>NMB</sub> NMB +/- 1.96 (SEc<sup>2</sup> + (W SEq<sup>2</sup>) – 2 W ρ SE<sub>c</sub> SE<sub>q</sub>) <sup>0.5</sup>
- If we set CI = 0, we can derive NMB CI equation from Fieller's theorem equation

