Sample Size and Power for Cost-Effectiveness Analysis

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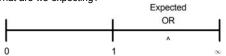
Outline

- Goals of sample size and power analysis
- · Sample size
 - Formula
 - Similarities to and differences from clinical SS&PA
 - · Correlation of difference
 - · Willingness to pay
 - · Standard deviations of cost and effect
- Power
 - Formula
 - Patterns of power
- (Briefly) Where to obtain the data
- Appendix: Sampling Uncertainty for Cost-Effectivenes



Goal of Clinical Sample Size Calculation

- Suppose we've estimated sample size for a change in odds of occurrence of a clinical outcome using α = 0.05 and power = 0.8
- · What are we expecting?





Goal of Clinical Sample Size Calculation (2) • Expectation: Among repeated experiments, ORs' 95% CI exclude 1 from above in 80% of experiments and either include 1 or exclude 1 from below in 20% of experiments Expected OR 0 1 0

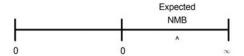
Goal of Cost Effectiveness Sample Size Calculation Suppose we've estimated sample size for assessing cost-effectiveness using α = 0.05 and power = 0.8 What are we expecting? Expected CE Ratio Λ



Cost Effectiveness Ratio • Expectation: Among repeated experiments, ICERs' 95% CI exclude WTP/W from below in 80% of experiments and either include W or exclude W from above in 20% Expected CE Ratio WTP



 Expectation: Among repeated experiments, NMBs' 95% CI exclude 0 from above in 80% of experiments and either include 0 or exclude 0 from below in 20%





Goal of Sample Size and Power Calculation

- More generally, sample size and power calculations allow us to conduct experiments with an expected likelihood that at conclusion of experiment we will be able to be confident in resulting comparison of costs and effects
 - e.g., may hypothesize that point estimate for costeffectiveness ratio for therapy A will be 20,000 per QALY
 - May want to design an experiment that provides an 80% chance (i.e., power) of concluding with 95% confidence that therapy A is good value when we are willing to pay at most 75,000 per QALY



Sample Size / Power

- · Sample size calculation
 - Given a desired alpha (α) and power $(1\text{-}\beta),$ proactively manages probability of saying a difference exists when none does
 - Type 1 error; False positive; alpha; confidence
- · Power Analysis
 - Given a desired alpha and a known sample size, proactively manages probability of saying no difference exists when one does
 - Type 2 error; False negative; (1-Beta); power
- "provides an 80% chance (power) of concluding with 95% confidence (alpha) that therapy is good value"



Other Cost-Effectiveness Sample Size Traditions

- Sample size approach described here comes out of frequentist statistical tradition
- Other approaches that have been discussed in costeffectiveness literature include:
 - Bayesian (O'Hagan and Stevens)
 - Value of information (Koerkamp et al.)
 - Opportunity cost (Gafni et al.)
 - Decision model (Willan and O'Brien)



Sample Size Formula, Common SDs

Assuming equal SDs and sample sizes, sample size formula is:

$$n = \frac{2 \left(z_{\alpha} + z_{\beta}\right)^{2} \left(sd_{c}^{2} + \left(W sd_{q}\right)^{2} - \left(2 W \rho sd_{c} sd_{q}\right)\right)}{\left(W\Delta Q - \Delta C\right)^{2}}$$

where n = sample size/group; z_α and z_β = z-statistics for α (e.g., 1.96) and β (e.g., 0.84) errors; sd = standard deviation for cost (c) and effect (q); W = maximum willingness to pay we wish to rule out; and ρ = correlation of difference in cost and effect; and (W Δ Q- Δ C) = NMB

www.uphs.upenn.edu/dgimhsr/stat-samps.htm



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Assumptions

Difference in costs: 200 Difference in effects: 0.01 Standard deviation, costs: 447.845 0.01326715 Standard deviation, effects: -0.71015 Correlation, difference in costs and effects: Willingness to pay: 75000 Two-tailed alpha level: 0.05 One-tailed beta level: 8.0

*** SAMPLE SIZE PER GROUP *** 95

http://www.uphs.upenn.edu/dgimhsr/eeinct_ssandp.htm



Sample Size Supports Other α / β Pairs

- Yes, 95 participants per group support α =0.05 and power=0.8
- But what enters formula is sum of z_α and $z_\beta~(z_\alpha+z_\beta)^2$ E.g., for $\alpha{=}0.05~$ and 1- $\beta{=}0.8,$ 2.8016 (1.96 + .8416)
- + 95 participants per group supports any z_{α}/z_{β} pair that has same sum, e.g.,:

Alpha	Z_{α}	Power	Zβ
0.01	2.5758	0.589	0.2258
0.03	2.1701	0.736	0.6315
0.05	1.9600	0.80	08416
0.075	1.7805	0.846	1.0211
0.10	1.6449	0.876	1.1567



Null Hypothesis, NMB

- Formula identifies a sample size that provides a 1- β % chance to have 1- α % confidence for rejection of null hypothesis that NMB (NMB = WQ C) calculated by use of W equals 0
 - If assumptions about C, Q, sd_c , sd_q , and ρ are correct and if α =0.05 and 1- β =0.8, then with a sample size of 95 per group:
 - In approximately 800 of 1000 repeated experiments, lower limit of 95% confidence interval for difference in NMB will be greater than 0 (therapy represents good value)
 - In approximately 200, 95% confidence intervals will either include 0 or have an upper limit less than 0 (no difference in or bad value)

Null Hypothesis, CER and Acceptability

- Formula also identifies a sample size that provides a 1- β % chance to have 1- α % confidence for rejection of null hypothesis that cost-effectiveness ratio equals W (i.e., that 1- α % confidence interval for cost-effectiveness ratio excludes W)
- Or equivalently, identifies a sample size that provides a 1- β % chance for rejection of null hypothesis that at W, fraction of joint distribution of difference in cost and effect that is acceptable is greater than $\alpha/2$ % and less than 1- $(\alpha/2)$ %



Similarities With Clinical Sample Size Formulas

Error

Rate

NMB Variance

$$n = \frac{2 (z_{\alpha} + z_{\beta})^{2} (sd_{c}^{2} + (W sd_{q})^{2} - 2 W \rho sd_{c} sd_{q})}{(W\Delta Q - \Delta C)^{2}}$$

$$n = \frac{2 (z_{\alpha} + z_{\beta})^{2} \left(sd_{q}^{2} \right)}{\Delta Q^{2}}$$

Difference²



Differences in Formulas

$$Var_{NMB} = sd_c^2 + (W sd_g)^2 - (2 W \rho sd_c sd_g)$$

- Variance of NMB more complicated than variance for usual continuous clinical differences
 - Includes $\rho,$ correlation of difference between cost and effect
 - Includes W, decision threshold we are trying to rule out



$$(sd_c^2 + (W sd_g)^2 - (2 W \rho sd_g sd_g))$$

- Correlation of difference in cost and effect indicates how changes in difference in cost are related to changes in difference in effect
 - Negative (win/win) correlation: larger differences in effects associated with smaller differences in costs
 - e.g., asthma care: reductions in exacerbations leads to lower costs
 - Positive (win/lose) correlation: larger differences in effects are associated with larger differences in costs
 - e.g., life-saving care: increases in stroke survival may lead to higher care costs
- If W is positive, all else equal, FEWER patients are needed when correlation is positive (win/lose) than when correlation is negative (win/win)



Effect of Correlation on Sample Size

• If Δ C=200, Δ Q=.01; SDc= 447.845; SDq=.01326715; W=75,000; α =0.05; and 1- β =0.8:

Correlation	Sample Size
-0.50	85
-0.25	74
0.00	62
0.25	51
0.50	39
0.75	28



Willingness to Pay and Identification of an Appropriate Outcome Measure

- Sample size calculations require stipulation of W for a unit of outcome
- In many medical specialties, researchers use disease specific outcomes
- Can calculate a cost-effectiveness ratio for any outcome (e.g., cost/case detected; cost/abstinence day)
- But to be informative, outcome must be one for which we have recognized benchmarks of cost-effectiveness
 - Argues against use of too disease-specific an outcome for economic assessment



W and Point Estimate

- When W is greater than expected point estimate, resulting sample size and power will allow us to be confident about value of MORE EFFECTIVE THERAPY
 - Because confidence statements from these trials will be that point estimate for more effective therapy is less than willingness to pay
- When W is less than expected point estimate, resulting sample size and power are for experiments that allow us to be confident that MORE EFFECTIVE THERAPY is bad value
 - Because confidence statements from these trials will be that point estimate is greater than willingness to pay

Effect of Willingness to Pay (W)

- · As already shown, direction of effect of correlation of difference is known
 - all else equal, more positive correlation, smaller sample size
- · For W, no such consistent relationship exists
- · Sample size approaches infinity as expected point estimate approaches W
 - e.g., if W = 75,000, expected ΔC =15,000, and expected ΔQ =0.2, NMB (W ΔQ -C) in denominator of sample size equation approaches 0
- · Sample size reaches a minimum at what I refer to as widest definable interval which is uniquely defined for an experiment based on $\Delta \text{C, SE}_{\text{c}},\,\Delta \text{Q. Se}_{\text{q}}.$ and ρ

"Expected" Sample Size Table, W

· Common expectation: all else equal, larger W yields smaller sample size

	Sample Size Per Group	
W	Exp 1 *	
20,000	3389	
30,000	1466	
50,000	592	
75,000	338	
100,000	252	
150,000	192	

^{*} ΔC=25; ΔQ=0.01; sd_c=2500; sd_q=.03; ρ=0.0; α=.05;



Sample Size Can Increase With Larger W

· Experiments can exist in which sample size increases as W increases

	Sample Size Per Group		
W	Exp 1	Exp 2*	
20,000	3389	371	
30,000	1466	421	
50,000	592	567	
75,000	338	777	
100,000	252	982	
150,000	192	1335	

^{*} ΔC =-1000; ΔQ =0.01; sd_c =5000; sd_q =.15; ρ =0.0; α =.05; 1- β =.8



Sample Size Not Necessarily Monotonic With W

• Experiments can exist in which sample sizes decrease and then increase as W increases

	Sample Size Per Group		
W	Exp 1	Exp 2	Exp 3*
20,000	3389	371	178
30,000	1466	421	158
50,000	592	567	151
75,000	338	777	153
100,000	252	982	156
150,000	192	1335	160

 * $\Delta C \! = \! .120; \; \Delta Q \! = \! 0.015; \; sd_c \! = \! 1000; \; sd_q \! = \! .05; \; \rho \! = \! 0.0; \; \alpha \! = \! .05; \; 1 \text{-}\beta \! = \! .8$



Effect of SD_q VS SD_c on Sample Size

- All else equal, increases in $\mathrm{SD_q}$ or $\mathrm{SD_c}$ lead to increases in sample size
- Commonly thought that sample size for costeffectiveness driven more by SD_c than by SD_q
 - If not, why do we commonly need a larger sample for cost-effectiveness outcome than for clinical outcome?
- However, if willingness to pay is substantially greater than SD_c, percentage changes in SD_q can have a substantially greater effect on sample size than will equivalent percentage changes in SD_c



Sample Size, SD_q , and SD_c

 Sample size formula is symmetric for SDs of cost and effect except for:

$$sd_{c}^{2} + (W sd_{g})^{2}$$

in numerator of equation

- * Square of SD_q is weighted by square of W (e.g., 75,000²); square of SD_c is unweighted
 - So long as W SD $_{\rm q}$ > SD $_{\rm c}$, SD $_{\rm q}$ will have a greater impact on sample size in face of equivalent percentage changes in SD $_{\rm q}$ and SD $_{\rm c}$
 - E.g., if W=75,000 and SD_q=0.2; percentage changes in SD_q will have larger effect so long as SD_c<15000 (75,000*0.2)

Sample Size Tables, Relatively Large SDc

 In this case with relatively larger SD_c's, equivalent percentage changes in SD_c and SD_q make no difference to required sample size for experiment

SD _c	N/Group	SD_q	N/Group
7500	390	0.1	390
15,000	635	0.2	635
22,500	1024	0.3	1024
30,000	1517	0.4	1517
45,000	3057	0.6	3057

 ΔC =250; ΔQ =.0.05; unless otherwise specified, sd_c=15,000 and sd_q=.2; p=-.1; W=75,000; α =.05; β =1-.8



Sample Size Tables, Relatively Small SD_c

 In this case with relatively smaller SD_c's, equivalent percentage changes in SD_c and SD_q yield substantially larger shifts in sample size given increases in SD_q

SD _c	N/Group	SD_q	N/Group
2500	306	0.1	114
5000	340	0.2	340
7500	389	0.3	710
10,000	455	0.4	1224
15,000	634	0.6	2685

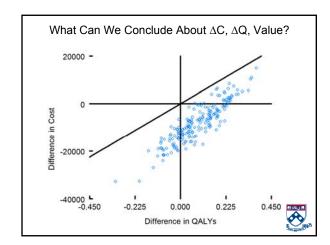
 ΔC =250; ΔQ =0.05; unless otherwise specified, sd_c= 5000 and sd_q=.2; ρ =-.1; w=75,000; α =.05; 1- β =.8



Economic Vs Clinical Sample Sizes

- Sample size required to answer economic questions typically considered larger than sample size required to answer clinical questions
 - But not necessarily in all cases
- ΔC and ΔQ are a joint outcome just as differences in nonfatal CVD events and all cause mortality are often combined into a joint outcome
- In same way that we can have more power for joint cardiovascular outcome than either individual outcome alone, we can have more power for cost-effectiveness than we do for costs or effects alone





Dropout and Sample Size

- Sample size estimates from formula appropriate if we expect no dropout from trial
- If we instead anticipate 10% dropout, divide sample size estimates by 0.9



Power Formula, Common SDs

· Assuming equal sds and sample sizes, power formula is:

$$z_{\beta} = \sqrt{\frac{n * (W\Delta Q - \Delta C)^{2}}{2 \left(sd_{c}^{2} + \left(W sd_{q}\right)^{2} - 2 W \rho sd_{q} sd_{c}\right)}} - z_{\alpha}$$

- Result is $\boldsymbol{z}_{\boldsymbol{\beta}},$ not power
- To estimate power, use normal distribution table to identify fraction of tail that is to left of z_{β}
 - Stata (V11+) code: power = normal(zbeta)
 - E.g., -1.96 = 2.5% power; -0.84 = 20% power; 0 = 50% power; .84 = 80% power; 1.28 = 90%



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Assumptions

200 Difference in costs: Difference in effects: 0.01 Standard deviation, costs: 447.845 Standard deviation, effects: 0.01326715 Correlation, difference in costs and effects: -0.71015 Willingness to pay: 75000 Two-tailed alpha level: 0.05 Sample size per group: 95

*** POWER TO DETECT DIFFERENCE *** 0.802 z beta: 0.8471

http://www.uphs.upenn.edu/dgimhsr/eeinct_ssandp.htm

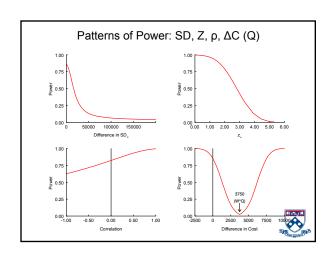


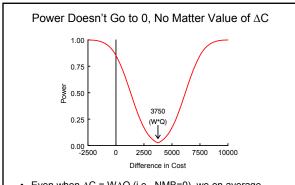
Power Table for Varying Sample Sizes

Sample Size	Power for W = 75,000
50	0.53
75	0.703
95	0.802
150	0.941
200	0.983

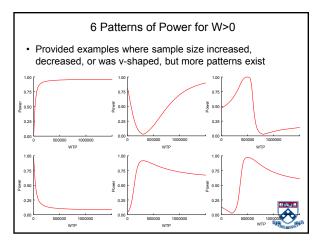
 ΔC =200; ΔQ =0.01; sd_c =447.845; sd_q =.01326715; ρ =-.71015; w=75,000; and α =.05

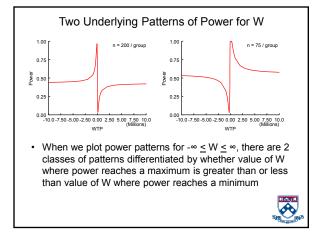






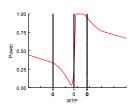
• Even when ΔC = W ΔQ (i.e., NMB=0), we on average will still accidentally conclude the therapy is good value 2.5% ($\alpha/2$) of time

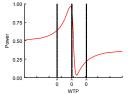




Truncation at 0 Creates 6 Patterns

• Can see 6 patterns for values of W>0 because W can equal 0 at any point on each of 2 curves





· Pattern we observe depends on where 0 W falls



Dropout and Power

 If we anticipate 10% dropout, we will want to use "effective sample size" (e.g., 0.9 * 95) when we make our power calculations



Where to Obtain Necessary Data?

- When therapies are already in use: Expected differences in outcomes and standard deviations can be derived from feasibility studies or from records of patients
 - Potential sources
 - Medical charts of administrative data sets
 - · Patient logs of their health care resource use
 - Asking patients and experts about kinds of care received by those with condition under study
 - Simple correlation between observed costs and effects may be an adequate proxy for measure of correlation used for estimating sample size



Obtaining Data for Novel Therapies

- For novel therapies, information about magnitude of incremental costs and outcomes may not be available
 - May need to be generated by assumption
 - Data on standard deviations for those who receive usual care/placebo may be obtained from feasibility studies or patient records
 - May want to assume sd from usual care (or a multiplier) will apply to new therapy, etc.



Summary

- Goal of sample size and power calculation for costeffectiveness analysis is to identify likelihood that an experiment will allow us to be confident that a therapy is good or bad value when we adopt a particular willingness to pay
- Sample size and power depend on difference in cost and effect, SD of cost and effect, correlation of difference, our willingness to pay, and our target confidence level



Summary (2)

- When we estimate sample size or power, we often do so for varying levels of W
 - Sample size is undefined / power reaches a minimum when W equals point estimate for cost-effectiveness ratio (NMB=0)
- When W is substantially greater than SD for cost, changes in SD for effect generally have greater impact on sample size than do changes in SD for cost
- So long as W>0, positive correlations decrease sample size / increase power

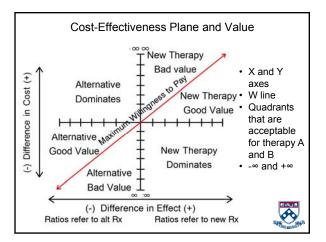


Sample Size Formula, SDs Differ When SDs differ, formula becomes: a, c ₁ , c ₂ , c ₃ , (a ₄ , c ₄ , c ₄), (w ² , a ₄ , c ₄		
effectiveness analysis (part 2). The effect of maximum willingness to pay. Pharmacoeconomics. 2011;29:287-96. Sample Size Formula, SDs Differ • When SDs differ, formula becomes: n = (z, z, y)^* ([ed_n^2 + ed_n^2) + [W^* (ed_n^2 + ed_n^2)^* (ed_n^2 + ed_n^2)^*]) (WAD - 26)^* where n = n/group; to/2 and tβ = t-statistics for a and β errors; sd = standard deviation for cost (c) and effect (Q); W = maximum willingness to pay one wishes to rule out; and p = correlation of difference in cost and effect	effectiveness analysis (part 1). Pharmacoeconomics.	
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errors; sd = standard deviation for cost (c) and effect (q); W = maximum willingness to pay one wishes to rule out; and ρ = correlation of difference in cost and effect	$ n = \frac{(z_a + z_{ji})^2 \ \left(\left(sd_{c0}^2 + sd_{c1}^2 \right) \ + \left(W^2 \ \left(sd_{q0}^2 + sd_{q1}^2 \right) \right) - \left(2 \ W \ \rho \ \left(sd_{c0}^2 + sd_{c1}^2 \right)^{0.5} \ \left(sd_{q0}^2 + sd_{q1}^2 \right)^{0.5} \right) \right)}{\left(W \Lambda Q - \Lambda C \right)^2} $	
Sampling Uncertainty Primer	errors; sd = standard deviation for cost (c) and effect (q); W = maximum willingness to pay one wishes to rule out; and ρ	
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Unidimensionality vs 2 Dimensionality

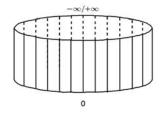
- Clinical outcomes typically are unidimentional and sampling uncertainty around these outcomes make sense on real number line
- Cost-effectiveness ratios are 2 dimensional and sampling uncertainty around these ratios can have unexpected properties on real number line
 - E.g., CI for ICER can include -∞ but -∞ needn't represent lower bound of interval; it can include ∞ but ∞ needn't represent upper bound of interval
- · Best to view results on 2D cost-effectiveness plane



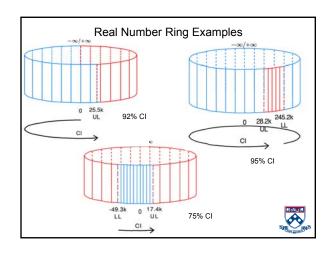


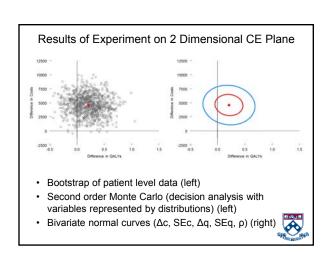
Real Number Ring

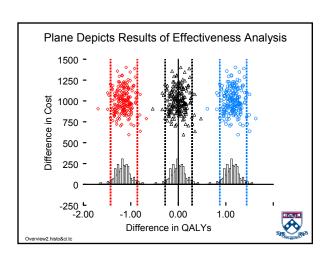
 If we want to move from CE plane to something like a real number line, overcome many problems if we map results onto real number ring

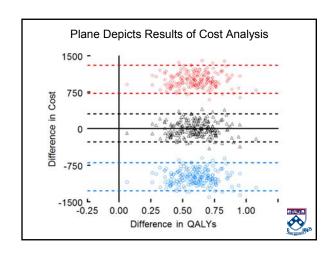


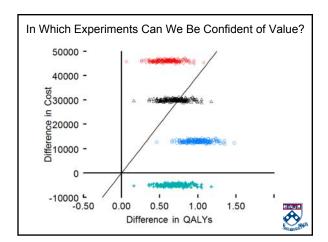












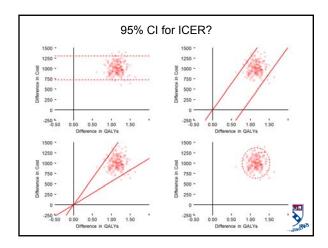
Red: confident of bad value All points above W line

Black, not confident of value Too many point on both sides of W line

Blue, confident of good value All points below W line and above \boldsymbol{X} axis

Cyan, confident of dominance All points in lower right quadrant





95% CI

Upper left: CI for ΔC

Upper right: CI for NMB

Lower right: 95% confidence ellipse around point on C/E plane defined by ΔC and Δq

(CE for point, not CI for ICER)

Lower left: 95% CI for ICER



Confidence Interval for ICER

- Because denominator of ratio can equal 0, there is no SE for ICER
- Thus CAN'T calculate ICER +/- 1.96 * $\mathrm{SE}_{\mathrm{ICER}}$
- CI for ICER defined as 0, 1, or 2 lines through origin of CE plane that exclude 2.5% of joint distribution of difference in cost and effect
- Fieller's theorem provides parametric equation for calculating these CI:

 $\frac{(\Delta C \Delta E \cdot t_{\sigma l^2}^2 \rho s_{\Delta C} s_{\Delta E}) \pm ([\Delta C \Delta E \cdot t_{\sigma l^2}^2 \rho s_{\Delta C} s_{\Delta E}]^2 \cdot [\Delta E^2 \cdot t_{\sigma l^2}^2 s_{\Delta E}^2] [\Delta C^2 \cdot t_{\sigma l^2}^2 s_{\Delta C}^2])^{0.5}}{\Delta E^2 \cdot t_{\sigma l^2}^2 s_{\Delta E}^2}$



Net Monetary Benefit (NMB)

• NMB represents a transformation of ICER decision criterion (W > Δ C/ Δ Q becomes W Δ Q - Δ C > 0) which is linear and has a defined SE

 $SE_{NMB} = (SEc^2 + (W SEq^2) - 2 W \rho SE_c SE_q)^{0.5}$

- As with other differences, NMB is significant if it's CI excludes 0
- 95% CI_{NMB} = NMB +/- 1.96 * SE_{NMB} NMB +/- 1.96 (SEc 2 + (W SEq 2) – 2 W ρ SE $_c$ SE $_q$) $^{0.5}$
- If we set CI = 0, we can derive NMB CI equation from Fieller's theorem equation

